### Physics at the Tevatron

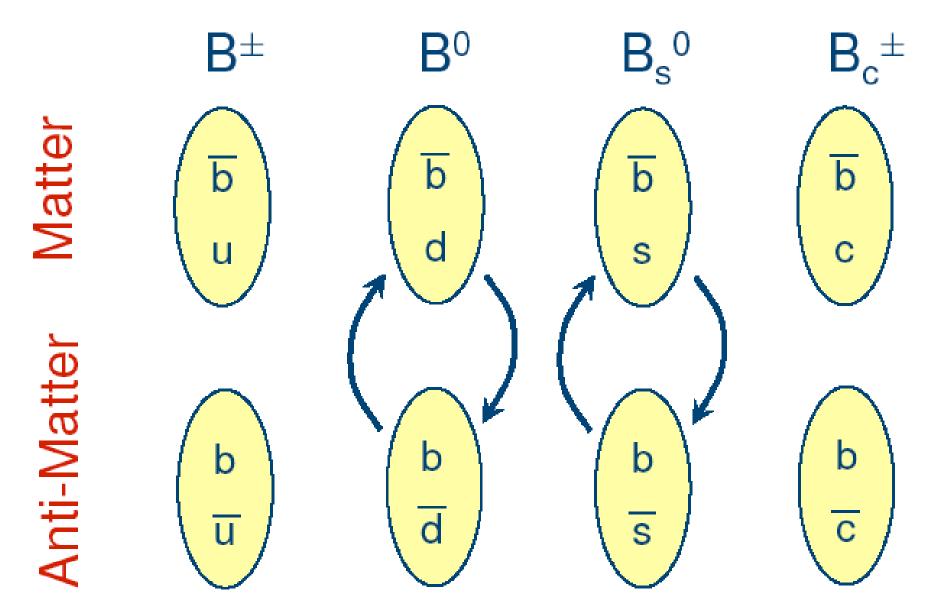
Lecture III

# Beate Heinemann University of Liverpool

#### **Outline**

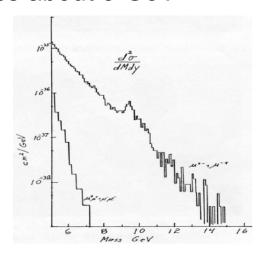
- Lecture I:
  - The Tevatron, CDF and DØ
  - Production Cross Section Measurements
- Lecture II:
  - Top Quark Mass and the Higgs Boson
    - jet energy scale and b-tagging
- Lecture III
  - B<sub>s</sub> mixing and B<sub>s</sub>→μμ rare decay
    - Vertex resolution and particle identification
- Lecture IV
  - Supersymmetry and High Mass Dilepton/Diphoton
    - Missing ET

#### B mesons

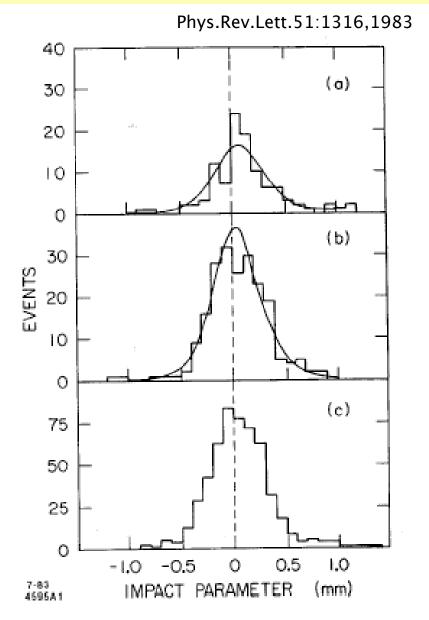


### History: B Mass and Lifetime

- Upsilon observation 1978
  - 3rd generation exists
  - Mass about 5 GeV

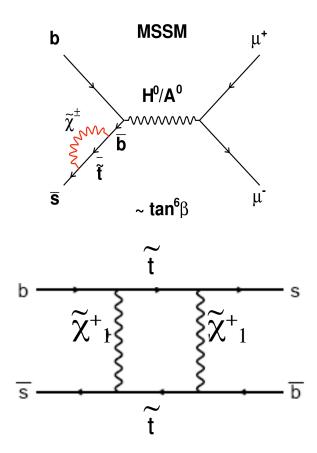


- Lifetime observation 1983:
  - Lifetime = 1.5 ps<sup>-1</sup>
  - Enables experimental techniques to identify B's



### Why B Physics?

- New physics could contribute to B-decays
  - SUSY particles can contribute in addition to SM particles
  - Z' bosons could also alter the effective couplings
- Complementary to direct searches



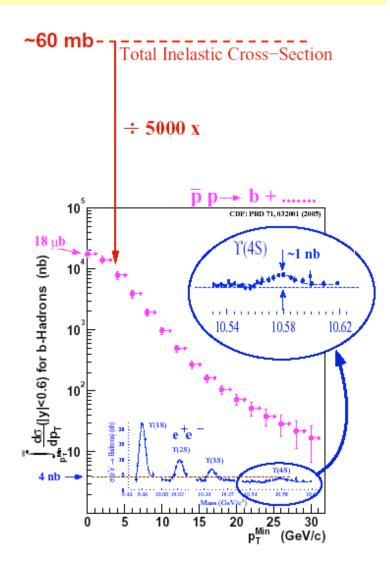
### B Physics at Hadron Colliders

#### • Pro's

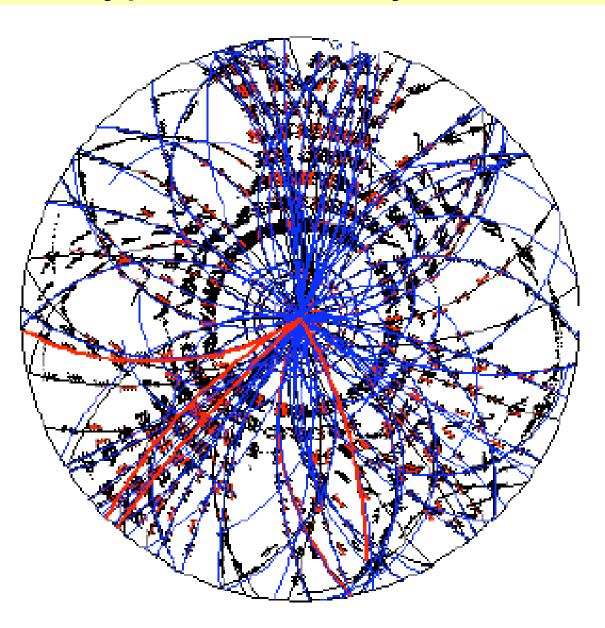
- Large cross section: 18 μb
  - 1000 times larger than at Bfactories
- Produce all B-hadron species:
  - $B^0$ ,  $B_s^0$ ,  $\Lambda_b$ ,  $B_c$ ,...

#### Con's

- No reconstruction of neutrals (photons,  $\pi^0$ 's)
- difficult to trigger, bandwidth restrictions
- Messy environment

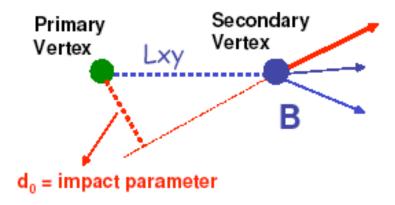


### A typical B-decay event



### The SVT Trigger at CDF

• trigger  $B_s \to D_s^-\pi$ ,  $B_s \to D_s^- I^+$ 

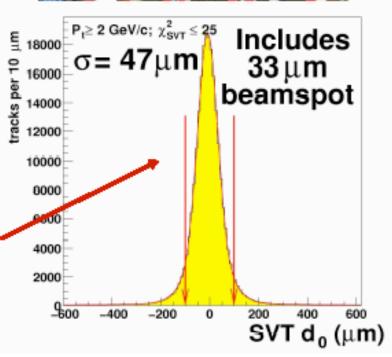


- trigger extracts 20 TB /sec
- "unusual" trigger requirement:
  - two displaced tracks:

 $(p_T > 2 \text{ GeV/c}, 120 \mu\text{m} < |d_0| < 1 \text{mm})$ 

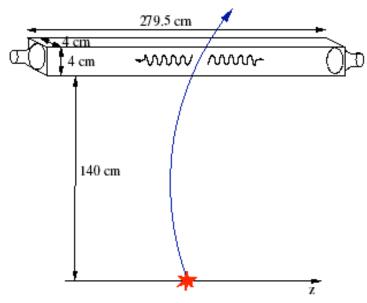
requires precision tracking in SVX

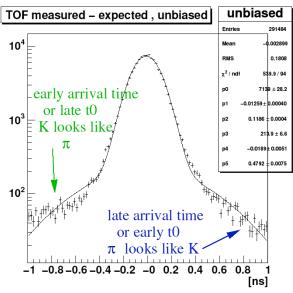




#### Particle Identification

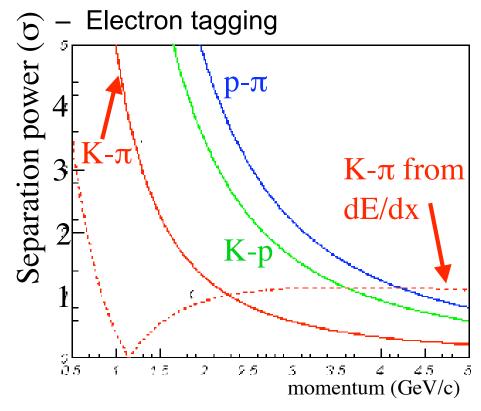
- TOF detector measures time of arrival in at r=140cm
  - Resolution 119 ps
  - Time depends on particle mass:
    - For M>0: v≠c
- Measure pulse height in COT, dE/dx:
  - lonization depends on particle species

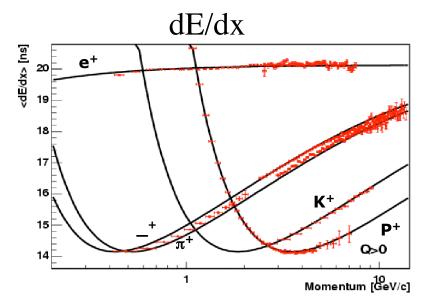


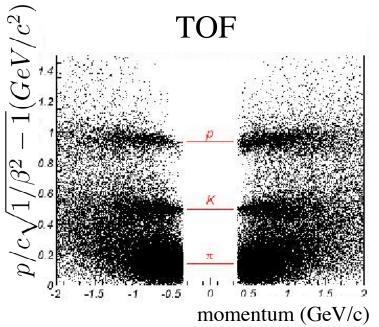


#### Particle Identification Results

- Separate kaons from pions
  - dE/dx gives 1σ separation for p>2 GeV
  - TOF gives better separation at low p
- Used for:
  - Kaon/pion separation

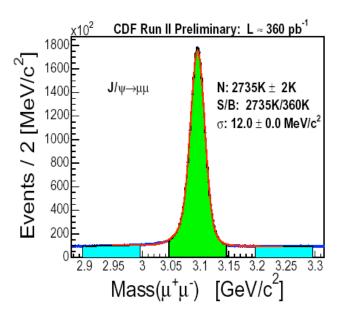




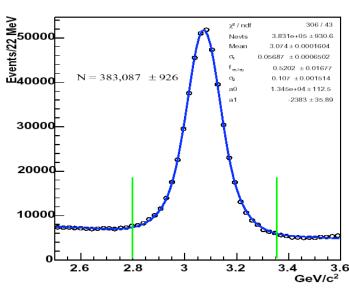


### J/Psi signals

- Superb calibration signal
- Yields:
  - CDF 2.7M / 360 pb<sup>-1</sup>
  - DØ: 0.4M / 250 pb<sup>-1</sup>
- Mass resolution ~1%
  - CDF: 12 MeV
  - DØ: 60 MeV
- Used to calibrate:
  - Magnetic field
  - Detector material
  - Momentum resolution
  - Hadron calorimeter



J/ψ Invariant Mass

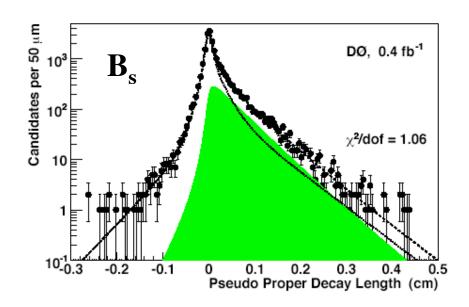


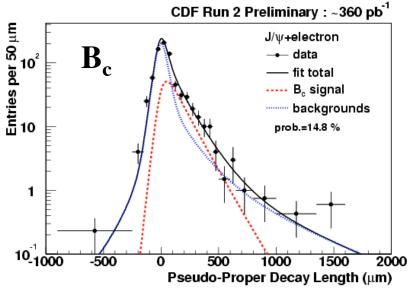
### Lifetime Measurements: $B_s^0, \Lambda_b, B_c$

Measure lifetimes of many B hadrons:

$$\lambda_B = \frac{L_{xy}}{(\beta \gamma)_T^B} = L_{xy} \frac{cM_B}{p_T},$$

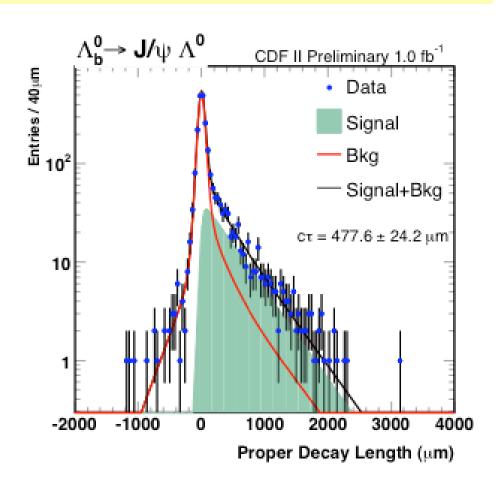
- Why?
  - Tests theoretical predictions:
    - Electroweak and strong sector play role
  - Demonstrates
     understanding of vertex
     resolution/detector
    - Important for both low and high P<sub>T</sub> physics programme





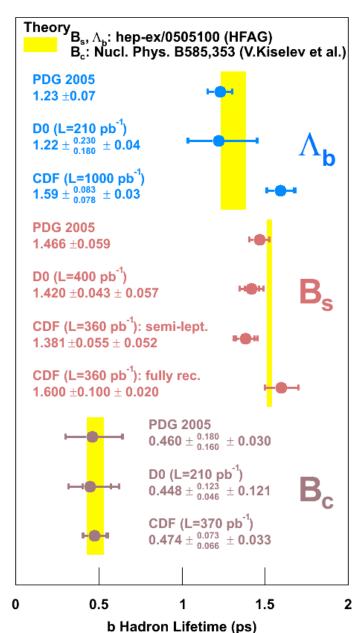
### $\Lambda_{b}$ Lifetime

- Standing puzzle at LEP
  - Why is the lifetime so much shorter than that of the other B mesons
  - Measurement were mostly made in semileptonic decays due to low stats
- New at Tevatron
  - Measurements in fully hadronic decay modes
  - Indication it may be higher in those modes
- Are we missing anything in semileptonic decays
  - Other than the neutrino????



### Summary of Lifetimes

- Good agreement with PDG world average
  - Mostly LEP data
  - Precision similar
- Theoretical predictions mostly confirmed
- Outstanding questions
  - Is B<sub>s</sub> lifetime really shorter than B<sub>d</sub> lifetime?
  - Is  $\Lambda_b$  lifetime really shorter?
  - Are the semileptonic measurements systematically lower than the hadronic ones?
- Will be answered with increasing data samples



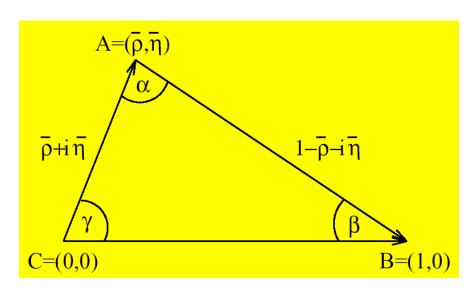
## B<sub>s</sub> mixing

### Cabibbo-Kobayashi-Maskawa Matrix

#### CKM Matrix Wolfenstein parameterization

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{ud} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2 / 2 & \lambda & A\lambda^3 (\rho - i\eta) \\ -\lambda & 1 - \lambda^2 / 2 & A\lambda^2 \\ A\lambda^3 (1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

$$V_{ts} \sim \lambda^2$$
,  $V_{td} \sim \lambda^3$ ,  $\lambda = 0.224 \pm 0.012$ 



- Is this 3x3 matrix unitary?
  - 4th generation quarks?
  - New forces? E.g. SUSY?
- Measure each side and each angle:
  - Do all measurements cross at one point?

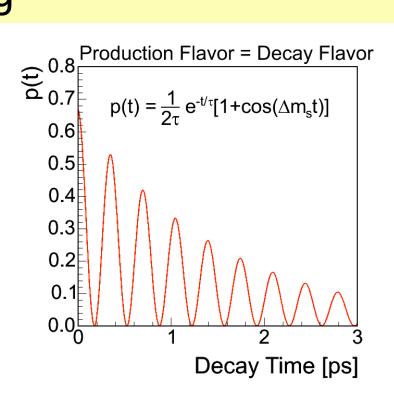
### **B** Mixing

Neutral B Meson system

$$|B>=(\overline{b}s);|\overline{B}>=(b\overline{s})$$

 Mass eigenstates are mixture of CP eigenstates:

$$|B_L\rangle = p|B^0\rangle + q|\overline{B}^0\rangle$$
 $|B_H\rangle = p|B^0\rangle - q|\overline{B}^0\rangle$ 
with  $|p|^2 + |q|^2 = 1$ 

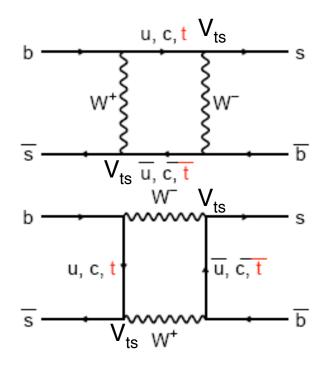


- B<sub>H</sub> and B<sub>L</sub> may have different mass and lifetime
  - $\Delta m = M_H M_L$  (>0 by definition)
  - $\Delta\Gamma$  =  $\Gamma_H$   $\Gamma_I$  where  $\Gamma$ =1/ $\tau$

• The case of  $\Delta\Gamma = 0$ 

$$p(B \to B) = \frac{e^{-t/\tau}}{2\tau} (1 + \cos \Delta mt)$$
$$p(B \to \overline{B}) = \frac{e^{-t/\tau}}{2\tau} (1 - \cos \Delta mt)$$

### B<sub>s</sub> mixing and the CKM Matrix

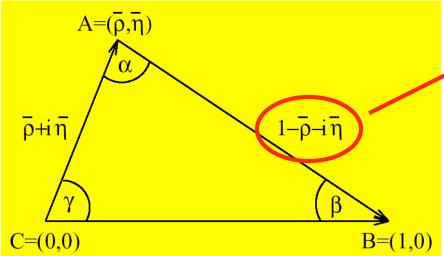


Ratio of frequencies for B<sup>0</sup> and B<sub>s</sub>

$$\frac{\Delta m_{s}}{\Delta m_{d}} = \frac{m_{Bs}}{m_{Bd}} \frac{f_{Bs}^{2} B_{Bs}}{f_{Bd}^{2} B_{Bd}} \frac{|V_{ts}|^{2}}{|V_{td}|^{2}} = \frac{m_{Bs}}{m_{Bd}} \xi^{2} \frac{|V_{ts}|^{2}}{|V_{td}|^{2}}$$

 $\xi$  = 1.210 +0.047 from lattice QCD (hep/lat-0510113)

$$V_{ts} \sim \lambda^2$$
,  $V_{td} \sim \lambda^3$ ,  $\lambda = 0.224 \pm 0.012$ 



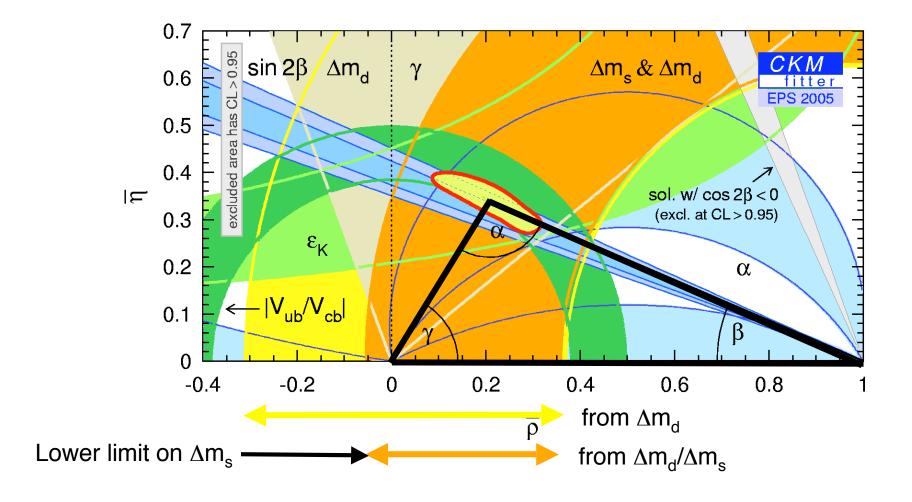
#### Constrain side of triangle:

$$|V_{td}|^2 = A^2 \lambda^4 \left[ (1 - \rho)^2 + \eta^2 \right]$$

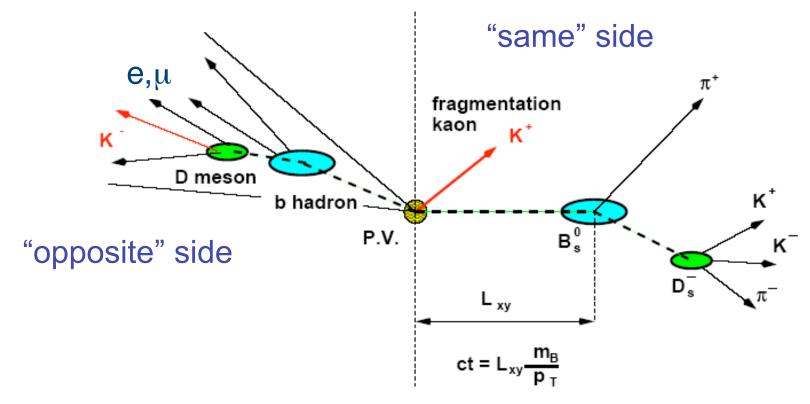
$$\frac{|V_{td}|^2}{|V_{ts}|^2} = (1 - \rho)^2 + \eta^2.$$

#### **Unitarity Triangle Fit**

- just for illustration, other fits exist
- CKM Fit result:  $\Delta m_s$ : 18.3<sup>+6.5</sup><sub>-1.5</sub> (1 $\sigma$ ) : <sup>+11.4</sup><sub>-2.7</sub> (2 $\sigma$ ) ps<sup>-1</sup>



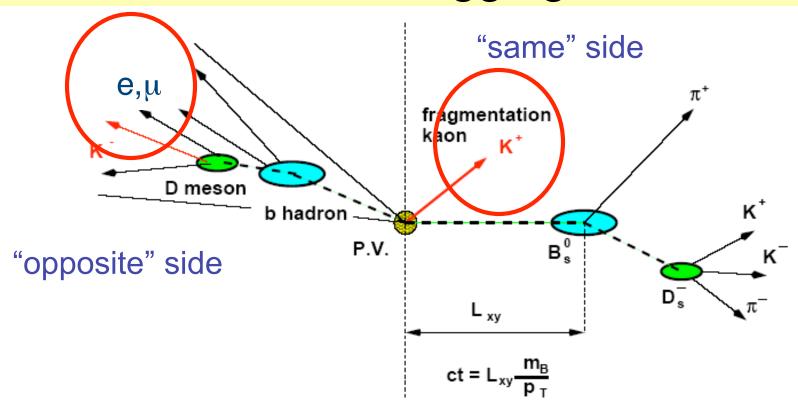
### The "Big" Picture



significance of measurement

$$\frac{1}{\sigma} = \sqrt{\frac{S\epsilon D^2}{2}} e^{-\frac{(\Delta m_s \sigma_t)^2}{2}} \sqrt{\frac{S}{S+B}}$$

### Flavour tagging



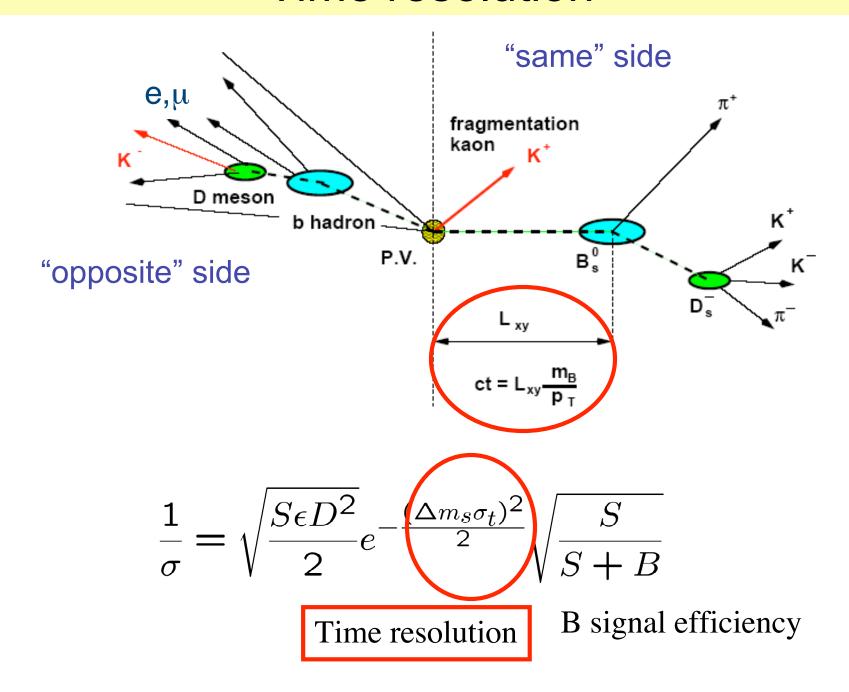
Time resolution

$$\frac{1}{\sigma} = \sqrt{\frac{S\epsilon D^2}{2}} e^{-\frac{(\Delta m_s \sigma_t)^2}{2}} \sqrt{\frac{S}{S+B}}$$

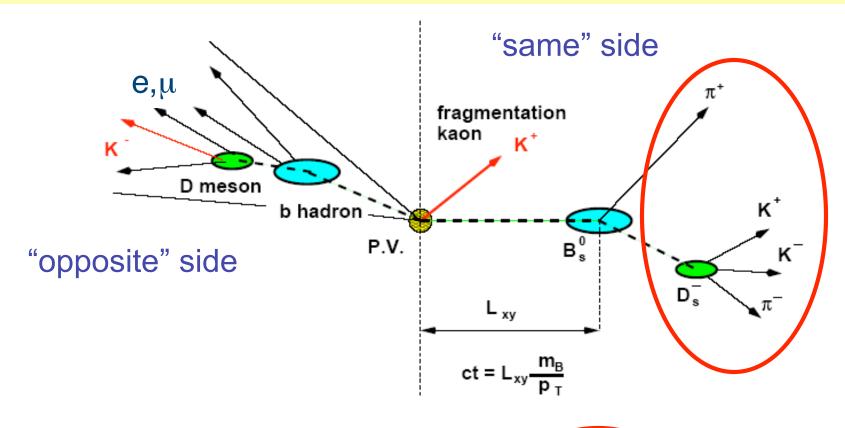
Flavour tagging

B signal efficiency

#### Time resolution



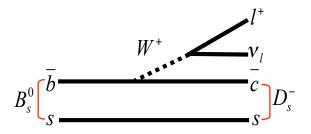
### Signal Identification



$$\frac{1}{\sigma} = \sqrt{\frac{S\epsilon D^2}{2}} e^{-\frac{(\Delta m_s \sigma_t)^2}{2}} \sqrt{\frac{S}{S+B}}$$

B signal reconstruction

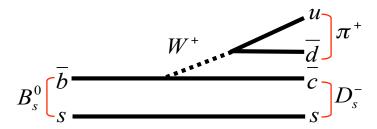
### Semileptonic vs Hadronic Decays



- Semileptonic:
  - High statistics:
    - 50K events
  - B momentum not known
    - Neutrino missing
    - Requires average correction factor K

$$ct = L_{xy} \frac{m(B)}{p_T(B)} = L_{xy} \frac{m(B)}{p_T(\ell D)} \cdot K$$

Poorer time resolution



- Hadronic:
  - Lower statistics:
    - 4K events
  - Full reconstruction of B momentum

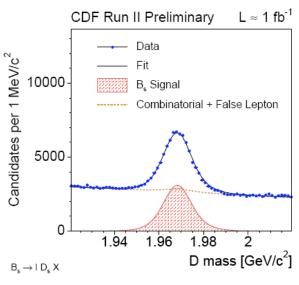
$$ct = L_{xy} \frac{m(B)}{p_T(B)}$$

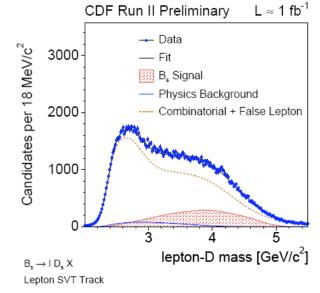
Excellent time resolution

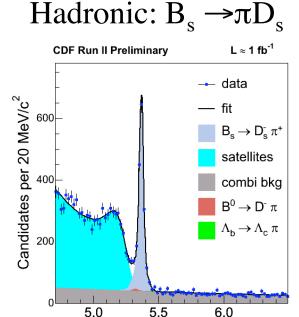
$$\sigma(ct) = \sqrt{(\sigma_0(ct))^2 + (ct \cdot \frac{\sigma(p)}{p})^2}$$

### Semileptonic and Hadronic Signals

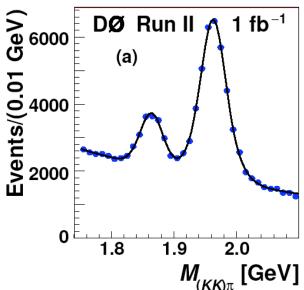
Semileptonic:  $B_s \rightarrow lvD_s$ 







Mass( $\phi(K^{\dagger}K^{-})\pi^{-},\pi^{+}$ ) [GeV/c<sup>2</sup>]



Semileptonic decays:

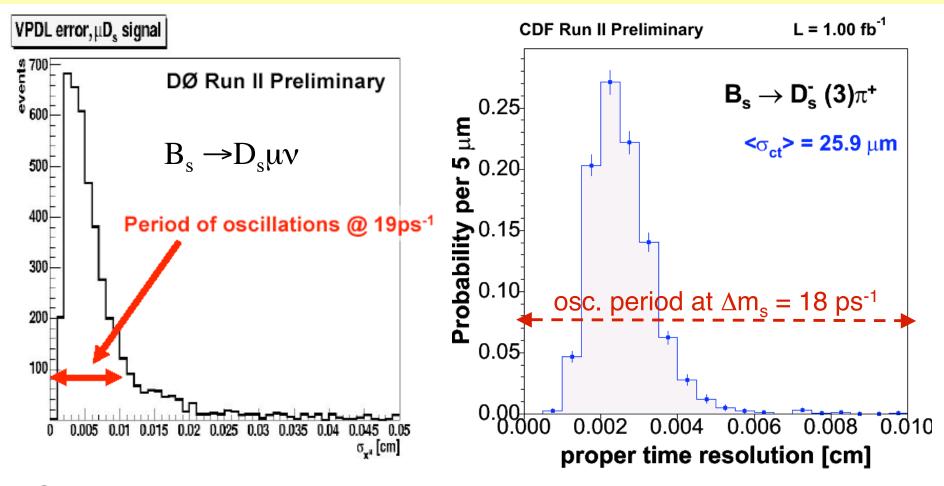
- DØ: ~27,000

- CDF: ~53,000

Hadronic Decays:

- CDF: ~3,700

### **Proper Time Resolution**

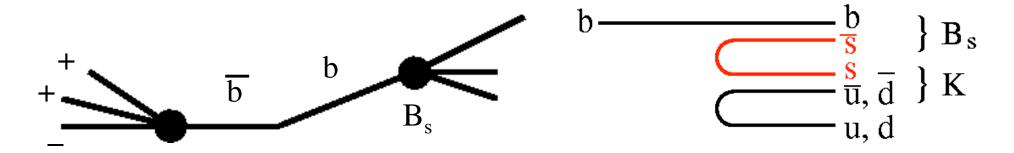


- Semileptonic Decays:
  - Resolution about 1 oscillation period
- Hadronic Decays:
  - Resolution 5 times better than 1 oscillation period

### **Production Flavour Tagging**

Opposite side tagging

Same side tagging

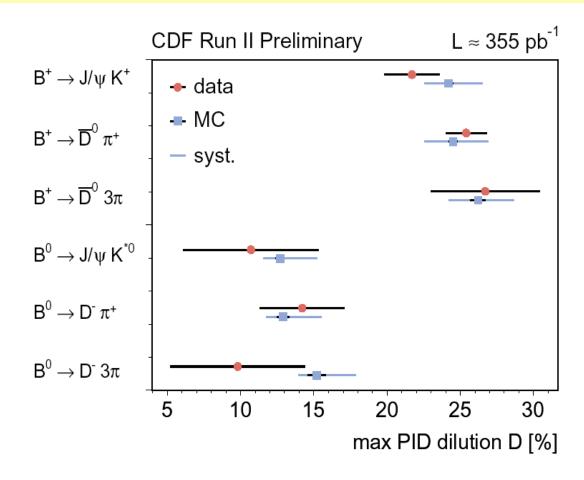


- Opposite side tags:
  - Only works for bb production mechanism
  - Used by CDF ( $\varepsilon D^2=1.5\%$ ) and DØ ( $\varepsilon D^2=2.5\%$ ):
    - · Lepton (muon or electron) or jet charge
- Same side tags:
  - Identify Kaon from B<sub>s</sub> fragmentation
  - CDF:  $\varepsilon D^2 = 3.5 4.0\%$
- Figure that matters: εD<sup>2</sup>
  - Efficiency ε of tagging (right or wrong)
  - Dilution D is fraction of correct tags

$$\epsilon = \frac{N_{tag}}{N_{all}}$$

$$D = \frac{N_{right} - N_{wrong}}{N_{tag}}$$

### Same Side Kaon Tagger Crosschecks

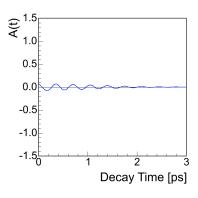


- Have to rely on MC to determine performance of Same Side Kaon Tagger
  - Extensive comparison of data and MC in high statistics B modes
- Good agreement between data and MC => confidence

### "Amplitude Scan": Measuring ∆m<sub>s</sub>

In principle: Measure asymmetry of number of matter and antimatter decays:

$$A(t) = \frac{N(B_s^0 \to B_s^0)(t) - N(B_s^0 \to \overline{B}_s^0)(t)}{N(B_s^0 \to B_s^0)(t) + N(B_s^0 \to \overline{B}_s^0)(t)} \propto \cos(\Delta mt)$$



In practice: use amplitude scan method

introduce amplitude to mixing probability

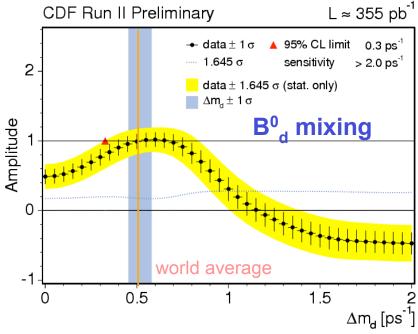
formula

$$P_{unmix}^{B_s} = \frac{1}{2} \Gamma_{B_s} e^{-\Gamma_{B_s} t} \left( 1 + A \cos \Delta m_s t \right)$$

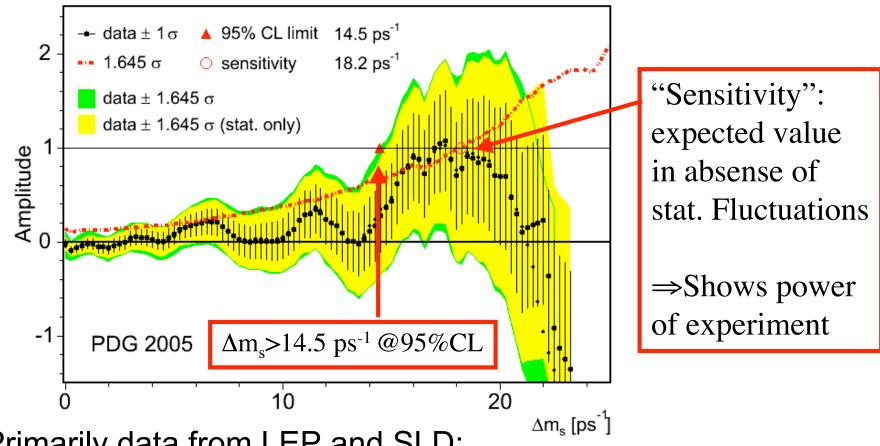
$$P_{mix}^{B_s} = \frac{1}{2} \Gamma_{B_s} e^{-\Gamma_{B_s} t} \left( 1 - A \cos \Delta m_s t \right)$$

- evaluate at each ∆m point
- Amplitude=1 if evaluated at correct ∆m
- Allows us to set confidence limit when  $1.645\sigma=1$

H. G. Moser, A. Roussarie, NIM **A384** (1997)

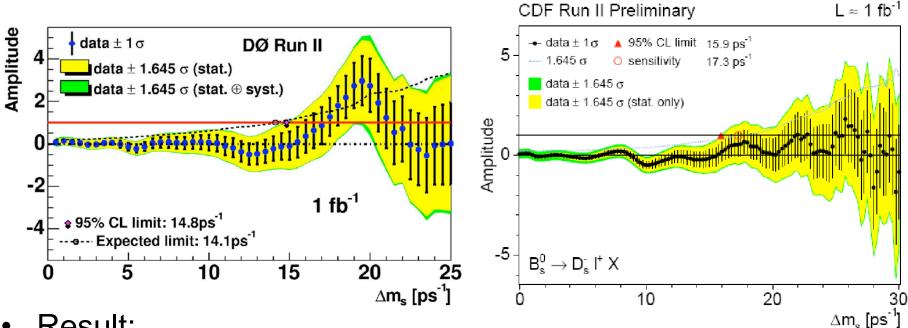


#### The World Data: PDG 2005



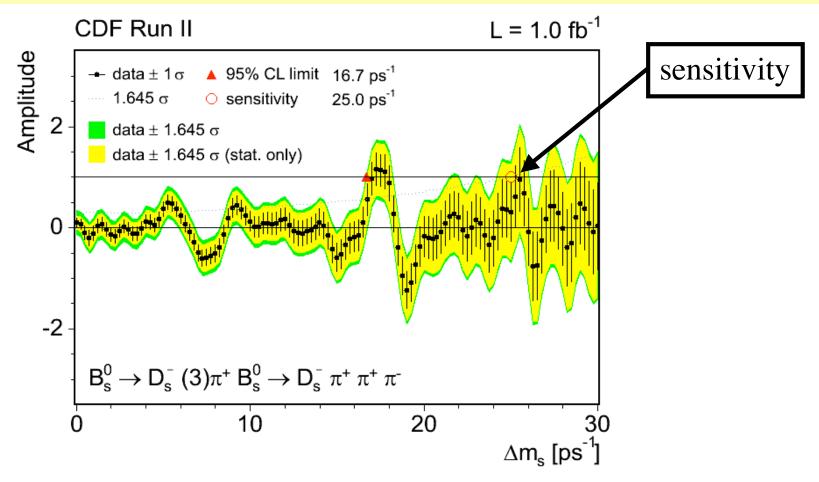
- Primarily data from LEP and SLD:
  - Consistent with no mixing within  $2\sigma$  everywhere
  - Consistent with mixing beyond 14.5 ps-1
    - Actual limit worse that sensitivity
    - either first hint of signal around 17-20 or statistical fluctuation
- Single best experiments sensitivity: ALEPH Δm<sub>s</sub>>10.9 ps<sup>-1</sup>

### Amplitude Scan: Semileptonic Decays



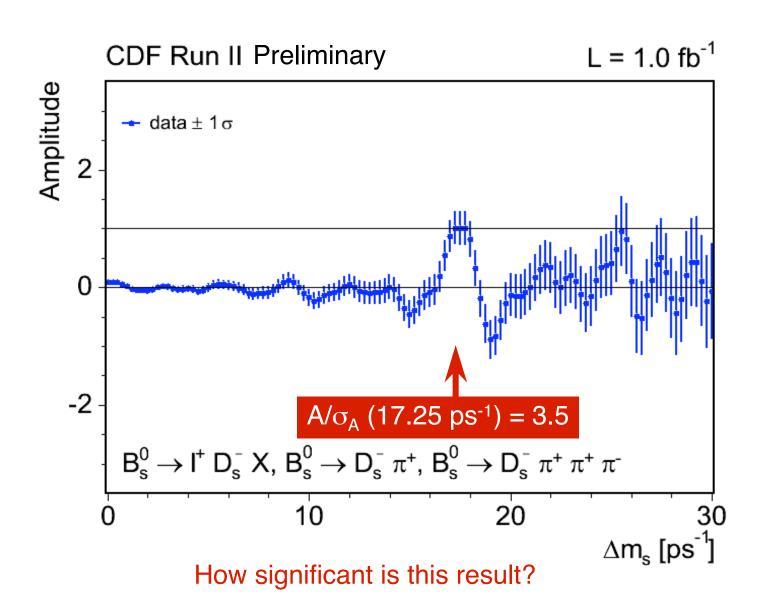
- Result:
  - DØ see high value at 19 ps<sup>-1</sup>
    - $2.5\sigma$  from 0: 1% probability to be consistent with no oscillations
    - 1.6σ from 1: 10% probability to be consistent with oscillation
  - CDF consistent with both oscillation and no-oscillation hypothesis within  $1\sigma$  for  $\Delta m_s > 15$  ps<sup>-1</sup>
- Sensitivity similar for CDF and DØ
  - this is a priori measure of analysis power
  - DØ: 14.1 ps<sup>-1</sup>, CDF: 17.3 ps<sup>-1</sup> (better than best experiment before)

### Amplitude Scan: Hadronic Decays

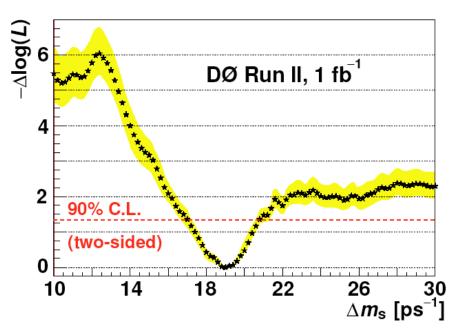


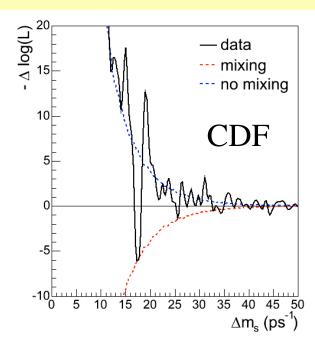
- CDF sees  $3.5\sigma$  oscillation signal at  $\Delta m_s = 17.3 \text{ ps}^{-1}$ 
  - Consistent with oscillations: A=1
  - Sensitivity: 25 ps<sup>-1</sup> (much better that the entire world data!)
- Use likelihood method to quantify signal and measure  $\Delta m_s$

### Combined CDF Amplitude Scan



#### Likelihood





- Likelihood ratio: ∆log(L) = log[ L(A=1) / L(A=0) ]
  - likelihood "dip" at signal
- Pseudo-experiments tell us how often this happens randomly:
  - DØ: 5.0+-0.3% within range of 16-22 ps<sup>-1</sup>
  - CDF: 0.5% anywhere at all
- Result:

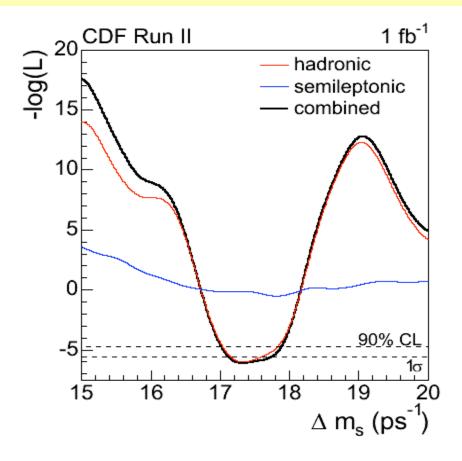
– DØ set 90% CL limit:

$$17 < \Delta m_s < 21 \text{ ps}^{-1}$$

– CDF measure:

$$\Delta m_{\rm s}$$
 = 17.33  $^{+0.42}_{-0.21}$  (stat)  $\pm$  0.07 (syst) ps<sup>-1</sup>

### Measurement of ∆m<sub>s</sub>

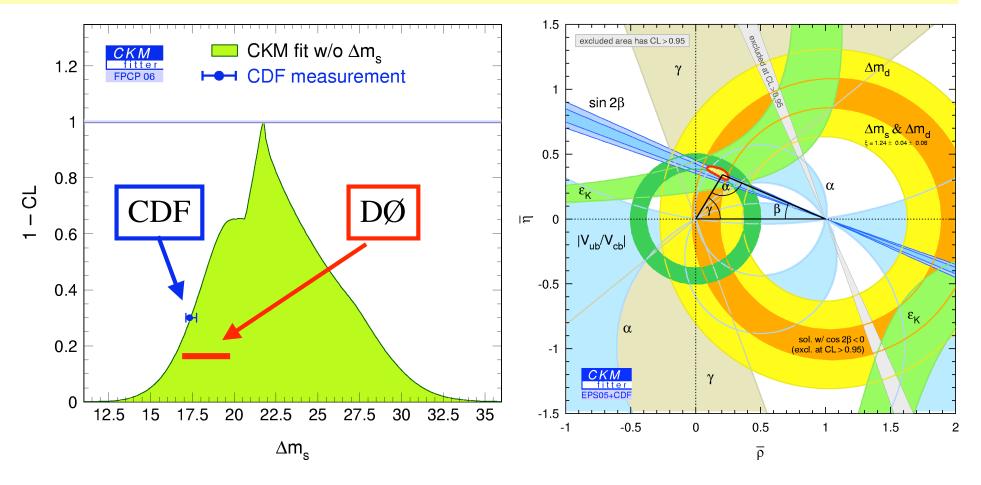


 $\Delta m_s = 17.33^{+0.42}_{-0.21} \text{ (stat)} \pm 0.07 \text{ (syst) ps}^{-1}$ 

the measurement is already very precise! ( at 2.5% level )

 $\Delta m_s$  in [17.00, 17.91] ps<sup>-1</sup> at 90% CL  $\Delta m_s$  in [16.94, 17.97] ps<sup>-1</sup> at 95% CL

### New Unitarity Triangle Fit



- Significant impact on Unitarity triangle understanding
- So far CKM matrix consistent with Unitarity: U+U=1

$$B_s \rightarrow \mu^+ \mu^-$$

# Rare Decay: B<sub>s</sub>→µ<sup>+</sup>µ<sup>-</sup>

SM rate heavily suppressed:

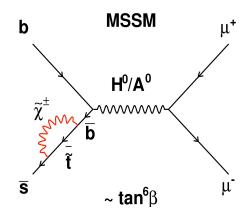
$$BR(B_s \to \mu^+ \mu^-) = (3.5 \pm 0.9) \times 10^{-9}$$
(Buchalla & Buras, Misiak & Urban)

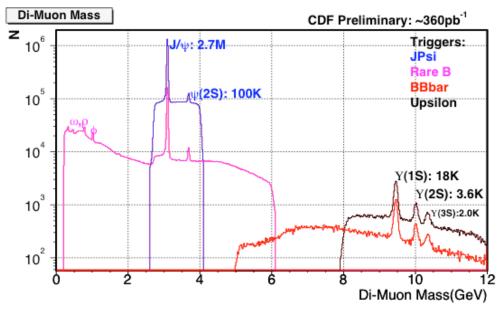
SUSY rate may be enhanced:

$$BR(B_s \to \mu^+\mu^-) \propto \tan^6 \beta/m_A^4$$
 (Babu, Kolda: hep-ph/9909476+ many more)



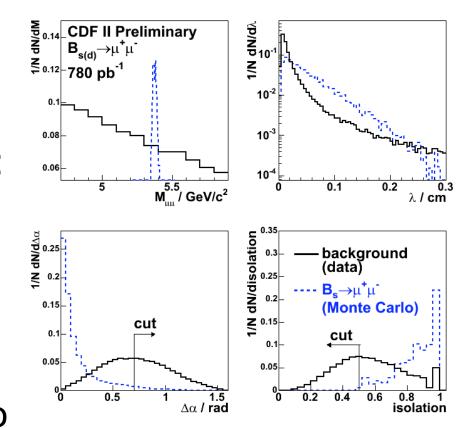
- Separate signal from huge background\
- Analysis is performed "blind"
  - First finalise cuts and background estimates
  - Only then look at data!
- More details on SUSY in lecture tomorrow



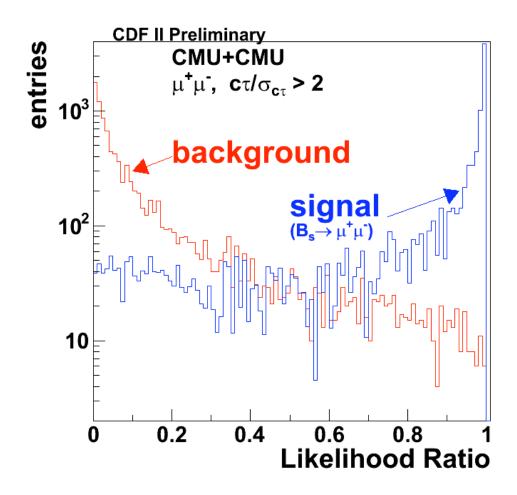


# $B_s \rightarrow \mu^+ \mu^-$ : Cut Optimisation

- Select 80,000 events with
  - 2 muons with p<sub>T</sub>>2 GeV
  - $P_T(\mu\mu) > 6 \text{ GeV}$
  - $-4.669 < M(\mu\mu) < 5.969 GeV$
- Discriminating variables:
  - 1. Dimuon mass
  - 2. Lifetime:  $\lambda$ =ct
  - 3. Opening angle between muons:  $\Delta\alpha$
  - 4. Isolation of B<sub>s</sub>
- Construct likelihood ratio using variables 2-4



## $B_s \rightarrow \mu^+ \mu^-$ : Likelihood ratio



Cut optimised to yield maximal Signal/√Bgd: L>0.99

# $B_s \rightarrow \mu^+ \mu^-$ : Background Prediction

#### Background:

- Random muons from cc and bb
- − QCD jets  $\rightarrow \pi/K \rightarrow \mu + X$
- Cannot estimate using MC => use "side bands"

#### Define control regions

- Lifetime<0 (due to misreconstruction): "OS-"
- Muons with same charge: "SS"
- Fake muons that fail certain ID cuts: "FM"

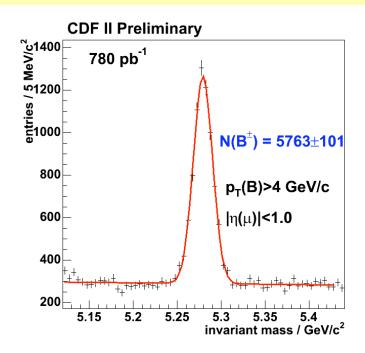
	Ī	CM	II C'M	TT T
		CMU-CMU		
$_{ m sample}$	$L_R  { m cut}$	$\operatorname{pred}$	obsv	$\operatorname{prob}(\%)$
	> 0.50	$489 \pm (12)$	483	41
OS-	> 0.90	$62 \pm (4)$	73	12
	> 0.99	$4.8 \pm (1.2)$	9	8
SS+	> 0.50	$5.4 \pm (1.3)$	4	40
	> 0.90	< 0.1	0	-
	> 0.99	< 0.1	0	-
SS-	> 0.50	$6.6 \pm (1.4)$	7	49
	> 0.90	$0.6 \pm (0.4)$	1	45
	> 0.99	< 0.1	0	-
FM+	> 0.50	$188 \pm (8)$	159	3
	> 0.90	$34 \pm (3)$		7
	> 0.99	$4.5 \pm (1.0)$	9	6

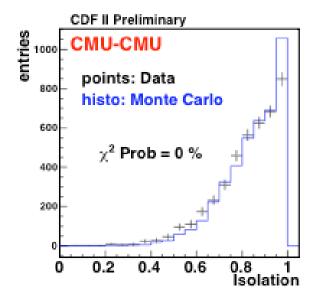
Data agree with background estimates in control regions

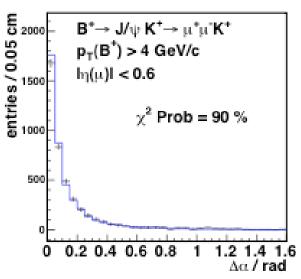
=> Gain confidence in background prediction!

## Signal Acceptance

- Does MC reproduce cut variables?
- Use B<sup>+</sup>→J/ψ+K<sup>+</sup> as control sample
  - E.g. test isolation cut of Iso>0.65
  - MC models data well
    - Disagreements taken as systematic uncertainty



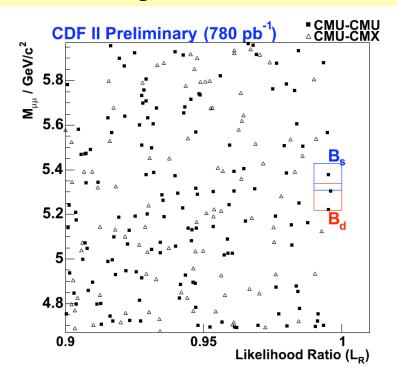


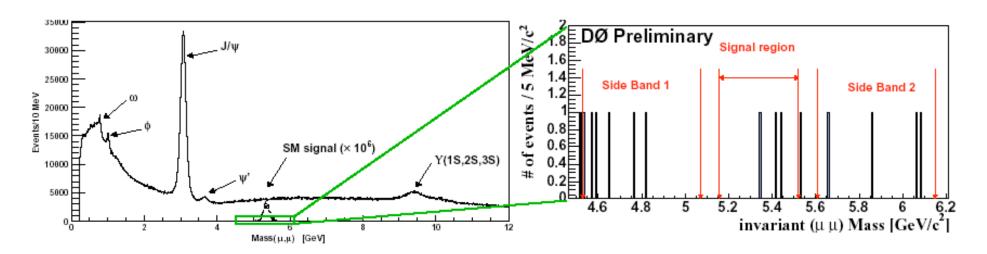


=> Let's open the blind box!

# Opening the "Box": $B_s \rightarrow \mu^+ \mu^-$

	DØ	CDF
Lumi (pb <sup>-1</sup> )	300	780
expected	3.7±1.1	1.3±0.4
observed	4	1





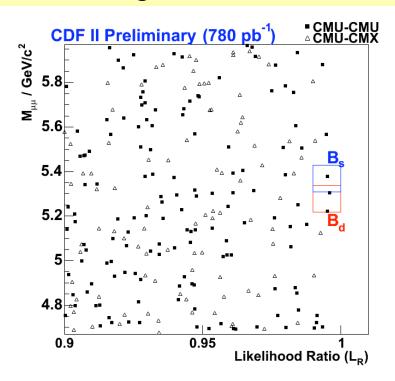
## Calculating a limit

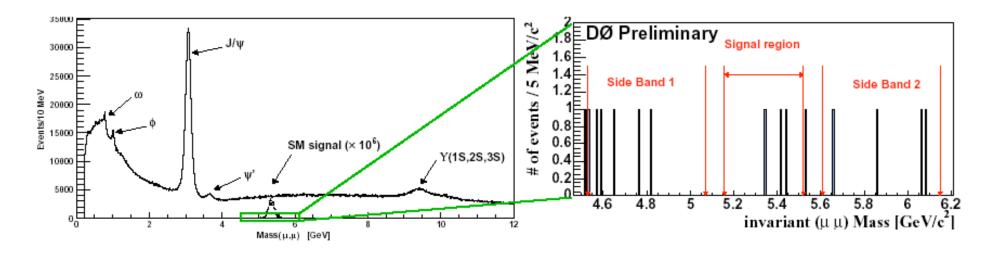
- Different methods:
  - Bayes
  - Frequentist
  - **—** ...
- Source of big arguments amongst statisticians:
  - Different method mean different things
  - Say what YOU have done
  - There is no "right" way
- Treatment of syst. Errors somewhat tricky

- But basically:
  - Calculate probability that data consistent with background + new physics:
    - P=e<sup>-μ</sup>μ<sup>N</sup>/N!
    - N = observed events
    - parameter  $\mu$  is  $N_{BG} + N_{new}$
    - P=5% => 95% CL upper limit on  $N_{new}$  and thus  $\sigma xBR=N_{new}/(\alpha L)$
- E.g.:
  - 0 events observed means <2.7 events at 95%C.L.</li>

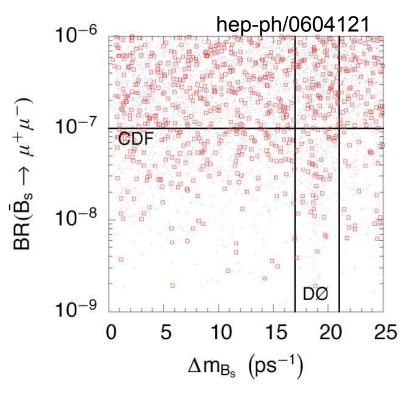
# Opening the "Box": $B_s \rightarrow \mu^+ \mu^-$

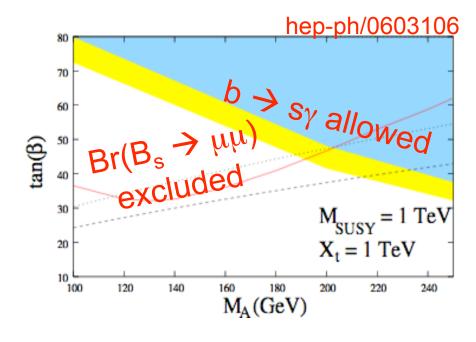
	DØ	CDF
Lumi (pb <sup>-1</sup> )	300	780
expected	3.7±1.1	1.3±0.4
observed	4	1
BR@95% C.L.	<3.7x10 <sup>-7</sup>	<1X10 <sup>-7</sup>





# What did we learn from B Physics about New Physics?





### SUSY contributions

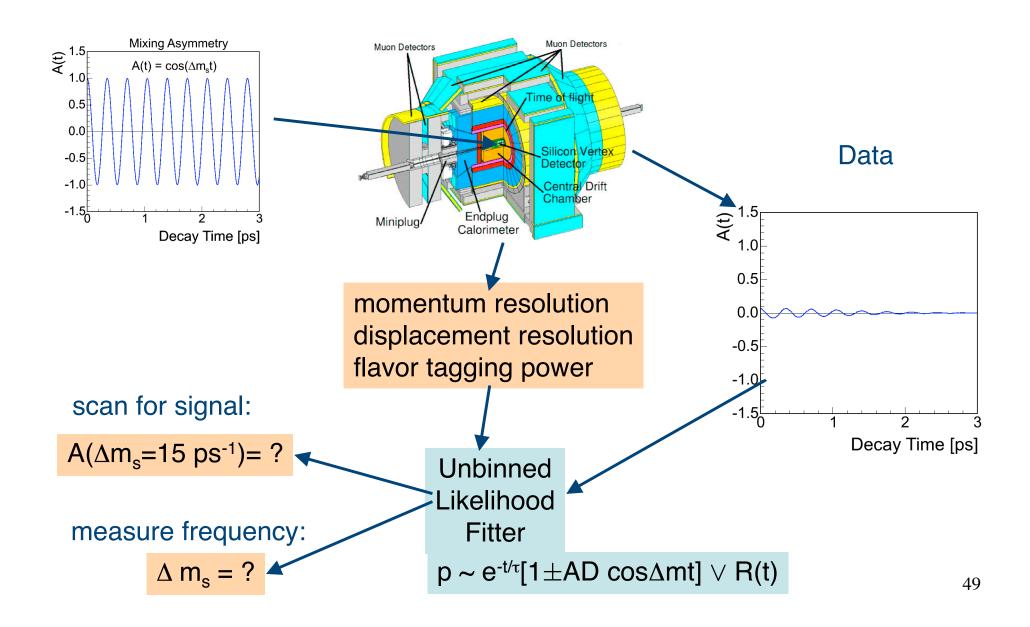
- affect both  $B_s$  mixing and  $B_s \rightarrow \mu^+\mu^-$
- Strong constraints on SUSY at large tanβ and small m<sub>A</sub>

## Conclusions

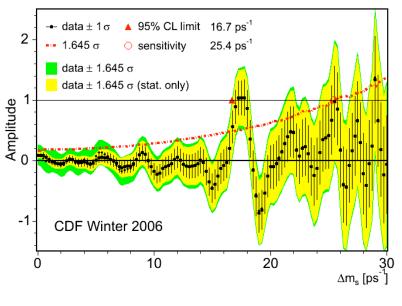
- New Physics could contribute to B hadron properties:
  - At hadron colliders
    - b-production cross section is 1000 times larger than at the B factories
    - all kinds of B hadrons are produced: B<sub>d</sub>, B<sub>s</sub>, Λ<sub>b</sub>, B<sub>c</sub>
      - The  $\Lambda_h$  lifetime is an interesting topic
  - First evidence of B<sub>s</sub> meson oscillations:
    - Measurement  $\Delta m_s = 17.33^{+0.42}_{-0.21}$  (stat)  $\pm 0.07$  (syst) ps<sup>-1</sup>
  - Search for B<sub>s</sub>→µµ yields strong limit
    - sensitive probe of New Physics
- No evidence for new physics contributions (yet)

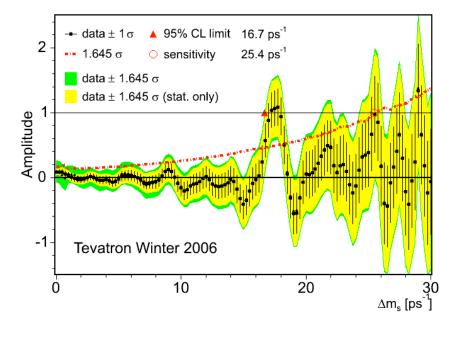
# Backup Slides

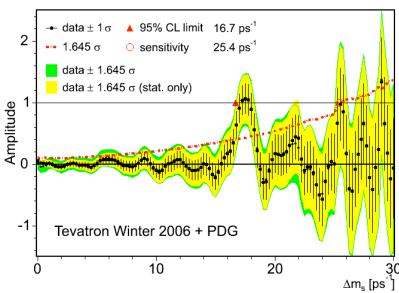
## Real Measurement Layout



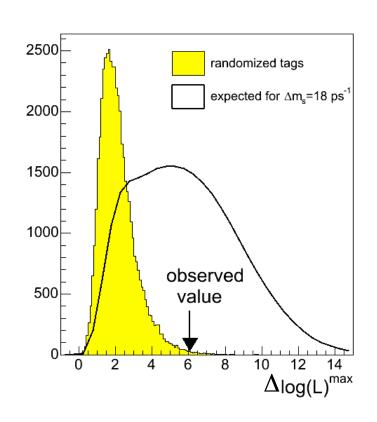
# Combining Tevatron with the World

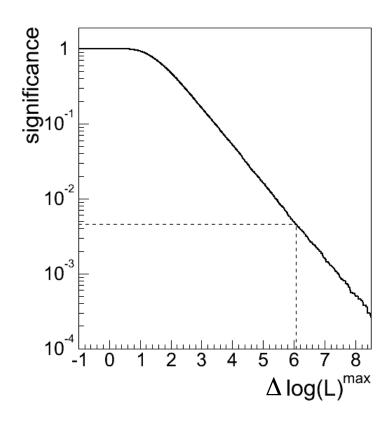






## Likelihood Significance





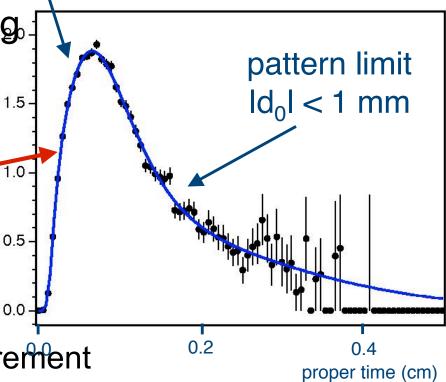
- randomize tags 50 000 times in data, find maximum ∆log(L)
- in 228 experiments,  $\Delta log(L) \geq 6.06$
- probability of fake from random tags = 0.5% → measure ∆m<sub>s</sub>!

## Hadronic Lifetime Measurement

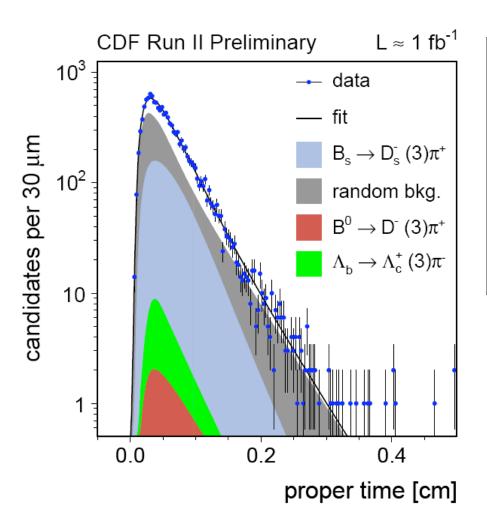
- SVT trigger, event selection sculpts lifetime distribution trigger turnon
- correct for on average using efficiency function:

 $p = e^{-t'/\tau} \vee R(t',t) \cdot ε(t)$ 

- efficiency function shape contributions:
  - event selection, trigger
- details of efficiency curve
  - important for lifetime measurement
  - inconsequential for mixing measurement



## Hadronic Lifetime Results



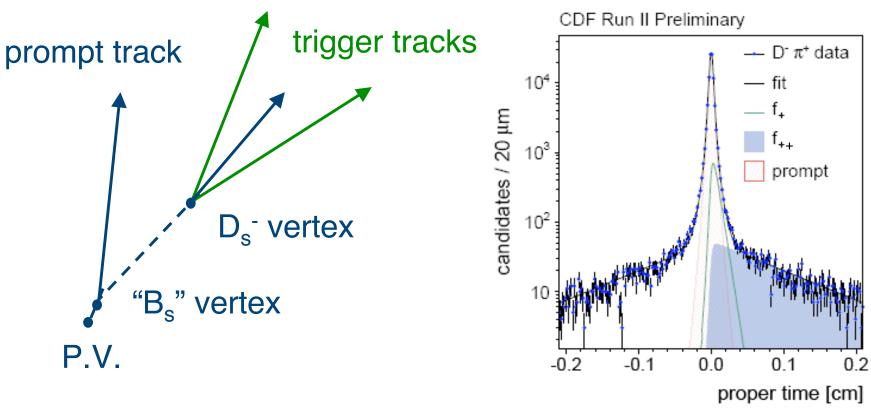
Mode	Lifetime [ps] (stat. only)	
$B^0  o D^{\scriptscriptstyle{-}}  \pi^{\scriptscriptstyle{+}}$	$1.508 \pm 0.017$	
$ extsf{B}^{ extsf{-}}  o  extsf{D}^0 \; \pi^{ extsf{-}}$	$1.638 \pm 0.017$	
$B_s \to D_s \ \pi(\pi\pi)$	$1.538 \pm 0.040$	

#### λ World Average:

$$\begin{array}{l} B^0 \to 1.534 \, \pm \, 0.013 \; ps^{\text{-}1} \\ B^+ \to 1.653 \, \pm \, 0.014 \; ps^{\text{-}1} \\ B_s \to 1.469 \, \pm \, 0.059 \; ps^{\text{-}1} \end{array}$$

#### **Excellent agreement!**

## Calibrating the Proper Time Resolution



- utilize large prompt charm cross section
- construct "B<sup>0</sup>-like" topologies of prompt D⁻ + prompt track
- calibrate ct resolution by fitting for "lifetime" of "B<sup>0</sup>-like" objects